

ON MULTI-MODULATION SCHEMES TO INCREASE THE RATE OF SPACE-TIME BLOCK CODES

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ABSTRACT

In this paper, multi-modulation schemes (MMSs) are employed to increase the rate of our two new Complex Orthogonal Designs (CODs) proposed for eight transmit antennas, namely C_1 and C_2 , corresponding to the Amicable Orthogonal Designs (AODs) $(8;1,1,2,2;1,1,2,2)$ and $(8;1,1,1,4;1,1,1,4)$, respectively. In addition, the optimal inter-symbol power allocation in the proposed codes in single modulation as well as in MMSs in Additive White Gaussian Noise (AWGN) channels is examined. It turns out that, in some modulation schemes, equal power transmission per each symbol time slot is not only optimal from the technical point of view, but also optimal in terms of achieving the best symbol error probability. The principles examining the MMSs in order to increase the rate of space-time block codes (STBCs) and the optimal power allocation for multi-modulated STBCs mentioned here can be generalized for STBCs of other orders without any difficulty.

1. INTRODUCTION

It is well known that STBCs of complex signals for more than two transmit antennas with full diversity cannot provide a full rate. The maximum rates of those STBCs for 4 and 8 transmit antennas are $3/4$ and $1/2$, respectively [1]. The STBCs for more than two transmit antennas are attractive in the sense that they provide more spatial diversity and temporal diversity for transmitted symbols, and consequently, provide better bit error performance than those for two transmit antennas. Additionally, they provide full spatial diversity for a given number of transmit antennas. To date, the existing STBCs for eight transmit antennas have comprised various unused symbol time slots (50% of symbol time slots are unused in the code mentioned in [1]), where no useful information is transmitted. The number of unused symbol time slots in STBCs should be limited since, during those slots, the transmit antennas must be turned off. This is inconvenient from technical point of views, especially for the systems transmitting a high data rate, i.e., the symbol time period is very small. In [2], two new orthogonal STBCs based on the AOD theory [3] were proposed for eight transmit antennas. In the proposed codes, namely C_1 and C_2 , the number of unused symbol periods is only 25% and 12.5%, respectively (see next section), compared to 50% in the conventional designs mentioned in literature, such as [1]. In addition, limiting the number of unused symbol time slots results in providing more space and symbol time slots for transmitting bits, i.e., providing more spatial and temporal diversity for those bits, and consequently, providing better bit error performance than the conventional code. This is clearly shown in the simulation results presented later in this paper. Moreover, the authors took advantage of the property that, some symbols in the proposed codes appear more often than the others, in order to increase the code rate by utilizing higher level modulation schemes with higher transmission power for those symbols appearing more times in the codes. In this paper, the authors provide further research on these codes. Particularly, we utilize an 8-ary Quadrature Amplitude Modulation (8 QAM) scheme to further improve the bit error performance of the proposed codes. In addition, we examine the optimal

inter-symbol power allocation in our proposed codes with various modulation schemes. It is a simple task to generalize the principles of the MMSs increasing the rate of STBCs and the optimal power allocation in multi-modulated STBCs mentioned in this paper to apply for STBCs of other orders, and therefore, we do not carry out this task here.

The paper is organized as follows. In Section 2, the two new STBCs proposed for eight transmit antennas are derived. In the next section, the MMSs increasing the rate of the proposed codes are examined. The optimal ratios of symbol power in different modulation schemes for C_1 and C_2 in AWGN channels are examined in Section 4. Simulation results are presented in Section 5 and the paper is concluded by Section 6.

2. TWO NEW ORTHOGONAL STBCS FOR EIGHT TRANSMIT ANTENNAS

Orthogonal STBCs that can be used with complex signal constellations can be constructed by using CODs defined as follows:

Definition 1 A complex orthogonal design (COD) X of order n is an $n \times n$ matrix on the complex indeterminates s_1, \dots, s_t , with entries chosen from $0, \pm s_1, \dots, \pm s_t$, their complex conjugates $\pm s_1^*, \dots, \pm s_t^*$, or their product with $i = \sqrt{-1}$, such that:

$$X^H X = \left[\sum_{k=1}^t |s_k|^2 \right] I_n \quad (1)$$

where X^H denotes the Hermitian transposition of X and I_n is the identity matrix of order n .

CODs are strongly connected to the AODs [3]. The detailed theory of AODs, including limitations on the number of different variables for a given design order can be found in [4]. Drawing from the presented theory of the existence of AODs, we found two new CODs of order 8, namely C_1 and C_2 (see Figure 1), corresponding to the AOD $(8;1,1,2,2;1,1,2,2)$ and AOD $(8;1,1,1,4;1,1,1,4)$, respectively. It is easy to realize that, C_1 and C_2 satisfy the following equation: $C_i^H C_i = \left[\sum_{j=1}^4 |s_j|^2 \right] I_8$, $i=1,2$. With single modulation, the proposed codes provide a code rate of $1/2$ as the conventional one.

3. MMS TO INCREASE THE CODE RATE

It is visible that, in C_1 and C_2 , some symbols are transmitted in more than a single time slot per given antenna. In fact, in C_1 , symbols s_3 and s_4 are transmitted twice as often as s_1 or s_2 . In C_2 , the symbol s_4 is transmitted four times as often as s_1, s_2 or s_3 . Thus, by associating s_3 and s_4 in C_1 and s_4 in C_2 with symbols from multilevel complex modulation schemes and the remaining symbols in each of C_1 and C_2 with QPSK symbols, the overall code rates can be increased (there is, certainly, a tradeoff between the rate increase and the bit error performance). Particularly, if the MMSs (QPSK+8 PSK) and (QPSK+16 QAM) are used, then the code rate increases from $1/2$ to $5/8$ and $3/4$ for C_1 , and to $9/16$ and $5/8$ for C_2 , respectively [2].

$$C_1 = \begin{bmatrix} s_1 & s_2 & \frac{s_3}{\sqrt{2}} & \frac{s_3}{\sqrt{2}} & 0 & 0 & \frac{s_4}{\sqrt{2}} & \frac{s_4}{\sqrt{2}} \\ -s_2^* & s_1^* & \frac{s_3^*}{\sqrt{2}} & -\frac{s_3^*}{\sqrt{2}} & 0 & 0 & \frac{s_4}{\sqrt{2}} & -\frac{s_4}{\sqrt{2}} \\ \frac{s_3}{\sqrt{2}} & \frac{s_3^*}{\sqrt{2}} & -s_1^R + is_2^I & -s_2^R + is_1^I & \frac{s_4}{\sqrt{2}} & \frac{s_4}{\sqrt{2}} & 0 & 0 \\ \frac{s_3}{\sqrt{2}} & -\frac{s_3^*}{\sqrt{2}} & s_2^R + is_1^I & -s_1^R - is_2^I & \frac{s_4}{\sqrt{2}} & -\frac{s_4}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & \frac{s_4}{\sqrt{2}} & \frac{s_4}{\sqrt{2}} & s_1 & s_2 & -\frac{s_3}{\sqrt{2}} & -\frac{s_3}{\sqrt{2}} \\ 0 & 0 & \frac{s_4}{\sqrt{2}} & -\frac{s_4}{\sqrt{2}} & -s_2^* & s_1^* & -\frac{s_3}{\sqrt{2}} & \frac{s_3}{\sqrt{2}} \\ \frac{s_4}{\sqrt{2}} & \frac{s_4}{\sqrt{2}} & 0 & 0 & -\frac{s_3}{\sqrt{2}} & -\frac{s_3}{\sqrt{2}} & -s_1^R + is_2^I & -s_2^R + is_1^I \\ \frac{s_4}{\sqrt{2}} & -\frac{s_4}{\sqrt{2}} & 0 & 0 & -\frac{s_3}{\sqrt{2}} & \frac{s_3}{\sqrt{2}} & s_2^R + is_1^I & -s_1^R - is_2^I \end{bmatrix}$$

$$C_2 = \begin{bmatrix} s_1 & 0 & s_3^R + is_2^I & s_2^R + is_3^I & \frac{s_4}{2} & \frac{s_4}{2} & \frac{s_4}{2} & \frac{s_4}{2} \\ 0 & s_1 & -s_2^R + is_3^I & s_3^R - is_2^I & \frac{s_4}{2} & -\frac{s_4}{2} & \frac{s_4}{2} & -\frac{s_4}{2} \\ -s_3^R + is_2^I & s_2^R + is_3^I & s_1^* & 0 & \frac{s_4}{2} & \frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} \\ -s_2^R + is_3^I & -s_3^R - is_2^I & 0 & s_1^* & \frac{s_4}{2} & \frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} \\ -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & s_1^R - is_3^I & s_2 & s_3^R - is_1^I & 0 \\ -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -s_2 & s_1^R + is_3^I & 0 & s_3^R - is_1^I \\ -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -s_3^R - is_1^I & 0 & s_1^R + is_3^I & -s_2^* \\ -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & -\frac{s_4}{2} & 0 & -s_3^R - is_1^I & s_2 & s_1^R - is_3^I \end{bmatrix}$$

Figure 1: Two new STBCs proposed for eight transmit antennas.

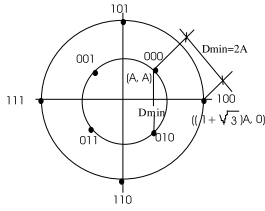


Figure 2: 8 QAM signal constellation and bit mapping scheme.

The transmission power in each symbol time slot is equally allocated and normalized to 1. It means that, s_3 and s_4 in C_1 are derived from a 2-power 8 PSK or 16-QAM signal constellation, while s_4 in C_2 is derived from a 4-power 8 PSK or 16-QAM signal constellation. All other symbols modulated by a QPSK signal constellation in the codes have unit power. Additionally, the MMS employing a QPSK signal constellation associated with an 8 QAM constellation (see Figure 2) can be utilized to further improve the bit error performance of the proposed codes C_1 and C_2 at the same bandwidth efficiency (same code rate) as when an 8 PSK signal constellation is used. Particularly, the symbols s_3 and s_4 in C_1 are modulated by a 2-power 8 QAM constellation, while s_4 in C_2 is modulated by a 4-power 8 QAM constellation. Other symbols in the codes are derived from a unitary QPSK constellation. The coordinates of the 8 QAM signal points, presented as functions of the factor A , are given in the figure. It is easy to realize that, if the Euclidean distance between the two closest symbols in the constellation is $D_{min}=2A$ then the average transmitted signal power is $P_{av}=4.73A^2$ [5]. For the 2-power and 4-power constellations, the value of A in Figure 2 is 0.65 and 0.9196, respectively. An 8 QAM signal constellation provides a better error property than an 8 PSK one, because, in order to have the same average power per symbol as in the former case, the Euclidean distance between the closest signal points in the later case d_{min} is smaller than that of the former case. Specifically, $d_{min}=1.665A$, i.e., $\frac{d_{min}}{D_{min}}=0.83$. Clearly, the orthogonality of the signals has been partially relaxed in the 8QAM constellation to increase the Euclidean distance between the closest signal points.

4. OPTIMAL INTER-SYMBOL POWER ALLOCATION IN SINGLE MODULATION AND MMSS

Allocating equally the power transmitted in each symbol period is optimal in terms of equal transmission among transmit antennas. However, in order to make sure whether the best error performance of the codes in different modulation schemes can be achieved, the

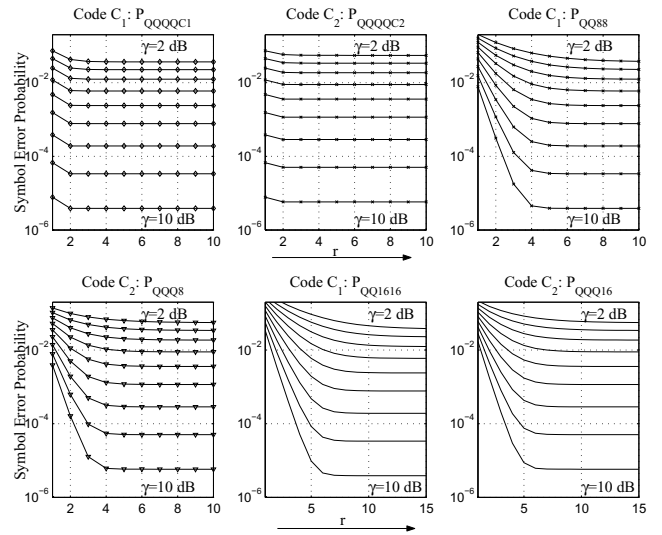


Figure 3: SER vs. r in single modulation and MMSs depending on γ in AWGN channels.

dependence of the error probabilities of the proposed codes on the ratio between the power of the symbols in the codes must be examined. In this section, the symbol error rates (SERs) of QPSK single modulation, (QPSK+8PSK) and (QPSK+16 QAM) MMSs are examined. The SERs of QPSK, 8PSK and 16 QAM symbols in AWGN channels are (see (5.2-59), (5.2-61) in [5] and (5.17), (5.18) and (5.19) in [6]):

$$P_{QPSK} = 2Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] \quad (2)$$

$$P_{8PSK} = 2Q(\sqrt{6\gamma_8 \sin \frac{\pi}{8}}) \quad (3)$$

$$P_{16QAM} = 3Q(\sqrt{\frac{4\gamma_{16}}{5}}) + Q(3\sqrt{\frac{4\gamma_{16}}{5}}) \quad (4)$$

where $Q(x) = \frac{1}{\sqrt{2\pi}} \int_x^\infty e^{-\frac{t^2}{2}} dt$; $\mu = \sqrt{\frac{2\gamma}{1+2\gamma}}$; γ , γ_8 and γ_{16} are the signal-to-noise ratio (SNR) per bit of QPSK, 8 PSK and 16 QAM symbols, respectively.

Next, we calculate the SERs of C_1 and C_2 in different modulation schemes. Let us consider the case where the symbols s_1 and

Table 1: The optimality of power allocation in single modulation and MMS

Modulation scheme	Min. r_{opt}	
	C_1	C_2
Single QPSK	2	2
QPSK + 8 PSK	6	4
QPSK + 16 QAM	12	8

s_2 in the code C_1 are QPSK modulated, while s_3 and s_4 are 8 PSK modulated as an example. It is noted that, in each row (or column) in C_1 , the power of the symbol s_j ($j=3,4$) transmitted is $|s_j|^2$, i.e., only one symbol s_j is transmitted, although, it may appear multiple times. Therefore, among four transmitted symbols, the probability when QPSK symbols are transmitted in C_1 is 50%, and that when 8 PSK symbols are transmitted is 50%, and consequently, the average SER of the code C_1 is:

$$P_{QQ88} = \frac{1}{2}P_{QPSK} + \frac{1}{2}P_{8PSK} \quad (5)$$

Let E_{s_k} be the average power of the symbol s_k , ($k=1..4$) and r be the inter-symbol power ratio of the proposed codes, which is defined $r = \frac{E_{s_i}}{E_{s_j}}$, where $i=3,4$; $j=1,2$ for C_1 and $i=4$; $j=1, \dots, 3$ for C_2 . Clearly, in MMSs, r is the ratio between the power of the higher level modulated symbols (8 PSK or 16-QAM) and that of the QPSK modulated ones. If we denote N_0 to be the variance of noise at the receive antenna, γ_s the average SNR per symbol and γ_b the average SNR per bit, then the power ratio can be rewritten as follows: $r = \frac{E_{s_i}/N_0}{E_{s_j}/N_0} = \frac{\gamma_{s_i}}{\gamma_{s_j}}$, where $\gamma_s = \gamma_b \log_2 M$ for an M-ary modulated symbol. Particularly, in the (QPSK+8PSK) MMS, $r = \frac{\gamma_{s_i}}{\gamma_{s_j}}$, ($i = 3, 4$; $j = 1, 2$), or:

$$r = \frac{3\gamma_8}{2\gamma} \quad (6)$$

Therefore, if average symbol error probabilities are presented as functions of r and γ (SNR per bit of QPSK modulated symbols), then from (2), (3), (5) and (6), we have the average SER of C_1 as given below¹:

$$P_{QQ88} = Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] + Q[\sqrt{4r\gamma}\sin(\pi/8)] \quad (7)$$

Similarly, the average SER for C_2 is:

$$P_{QQ08} = 1.5Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] + 0.5Q(\sqrt{4r\gamma}\sin(\pi/8))$$

Following this method to calculate symbol error probabilities, we derive the average SERs of QPSK single modulation and (QPSK+16QAM) MMSs in AWGN channels as:

- (QPSK+16QAM) multi-modulation:

$$\begin{aligned} P_{QQ1616} &= Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] + \\ &+ 1.5Q(\sqrt{0.4r\gamma}) + 0.5Q(3\sqrt{0.4r\gamma}) \\ P_{QQ016} &= 1.5Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] + \\ &+ 0.75Q(\sqrt{0.4r\gamma}) + 0.25Q(3\sqrt{0.4r\gamma}) \end{aligned}$$

¹The channel SNR, which is used to simulate in this paper and is defined in Section 5 as $SNR = \frac{\sum_{k=1}^4 E_{s_k}}{N_0}$, is a linear function of γ (for a given value r). Additionally, the symbol error probability is a monotonically decreasing function with respect to (w.r.t.) γ for a given value r (see (7) for instance). Hence, if the best error performance w.r.t. γ is achieved, then that w.r.t. SNR is also achieved. Based on these notes, in the paper, the authors search for the optimal inter-symbol power ratio r_{opt} w.r.t. γ , i.e., we search for the optimal power of the higher level modulated symbols corresponding to a given power of the QPSK modulated symbols.

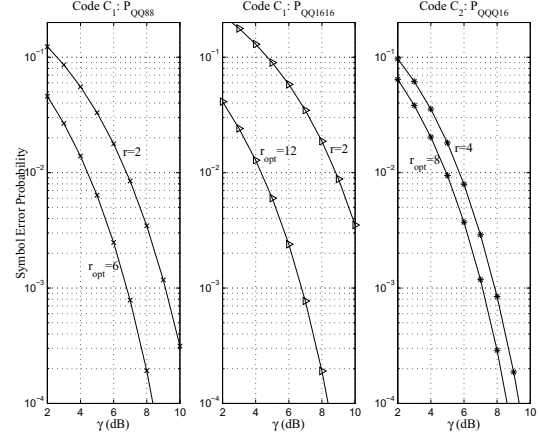


Figure 4: SER v.s. γ with the inter-symbol power ratio $r=2$ for C_1 , $r=4$ for C_2 and with the optimal values r_{opt} .

- QPSK single modulation:

$$\begin{aligned} P_{QQ00C_1} &= Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] \\ &+ Q(\sqrt{2r\gamma})[1 - 0.5Q(\sqrt{2r\gamma})] \\ P_{QQ00C_2} &= 1.5Q(\sqrt{2\gamma})[1 - 0.5Q(\sqrt{2\gamma})] \\ &+ 0.5Q(\sqrt{2r\gamma})[1 - 0.5Q(\sqrt{2r\gamma})] \end{aligned}$$

Figure 3 presents the theoretical relation between SERs and r depending on γ for the above modulation schemes. In this figure, γ runs from 2 dB to 10 dB. We can realize that, when r is small, then the higher r is, the better the performance is. However, when r increases, the curves become flat gradually. The value at which the curves become flat is the (smallest) optimal power allocation ratio r_{opt} . The optimal inter-symbol power ratios r_{opt} for C_1 and C_2 in different modulation schemes are presented in Tables 1. It is clear that the best symbol error performance can be achieved by the code C_1 in the QPSK single modulation, since, the power ratio of this code is $r=2$, which is equal to the (smallest) optimal power ratio $r_{opt}=2$. Similarly, the best symbol error performance is also achievable by the code C_2 in the QPSK single modulation and (QPSK+8 PSK) MMS, since, the power ratio of this code is $r=4$ while the (smallest) optimal power ratios are $r_{opt}=2$ and 4, respectively. For the remaining modulation schemes, $r < r_{opt}$ and, consequently, there exists the gap between the error performance curves corresponding to r and r_{opt} , which is presented in Figure 4. From that figure, we realize that, the potential improvements for the code C_1 in (QPSK+8PSK) MMS and (QPSK+16 QAM) MMSs are 2.5 dB and 4.5 dB, respectively. The potential improvement for C_2 in the (QPSK+16 QAM) MMS is 0.8 dB. The potential improvement is evaluated at $SER = 10^{-2}$. The potential improvement indicates that the error performance of the proposed codes, specially for C_1 in the (QPSK+16 QAM) MMS, can be much more improved by selecting r closed to r_{opt} with the penalty of unbalanced power transmission per symbol time slot at a given transmit antenna. In addition, it is observed from Figure 3 that, in the same MMS, the code C_1 may provide a higher code rate with a lower error probability than C_2 for large r ($r \geq 3$ in (QPSK+8PSK) MMS and $r \geq 5$ in (QPSK+16QAM) MMS) at any γ in the considered range (2-10 dB). Hence, it is preferable to select C_1 if r is large enough, provided that the balanced power transmission is not the necessary requirement of the system.

5. SIMULATION RESULTS

In this section, the bit error properties of the codes C_1 and C_2 in single modulation as well as MMSs are presented. A system comprising eight transmit antennas and one receive antenna is considered. SNR here means the channel SNR, i.e., the ratio

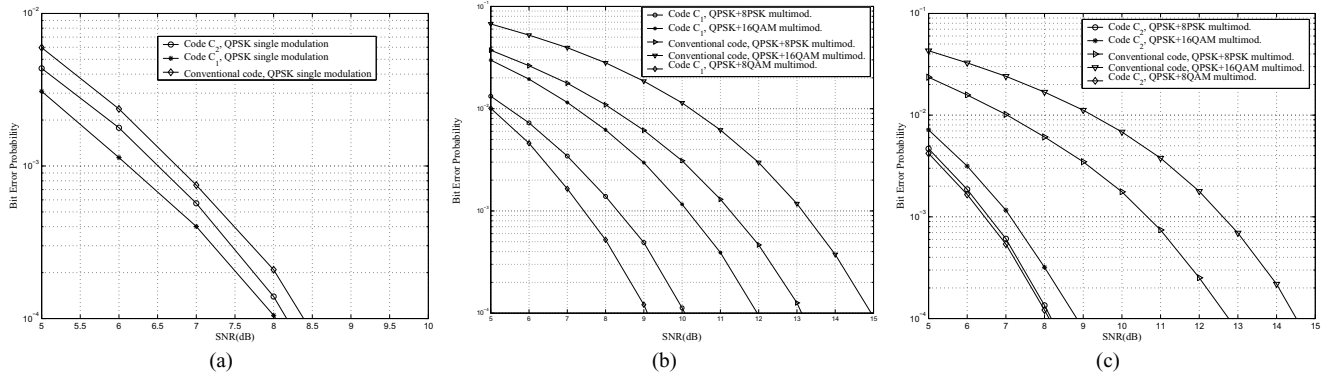


Figure 5: (a): Comparison between the proposed codes and the conventional one [1] with single QPSK modulation in AWGN channels; (b) and (c): Bit error performance of the code C_1 and C_2 with different MMSs in AWGN channels.

between the total power of the received signals and the power of noise during each symbol time slot. Channels are assumed to be AWGN ones. In all simulations, the power of the signal transmitted in each symbol time slot in C_1 and C_2 is normalized to one. Figure 5(a) indicates that, at bit error rate $BER=10^{-3}$, C_1 provides 0.4 dB bit error performance better than C_2 , and 0.65 dB better than the conventional code [1], when QPSK single modulation is considered. This is intuitively interpreted as follows. Code C_1 provides more diversity (temporal and spatial) for four bits embedded in the symbols s_3 and s_4 , while C_2 provides more diversity for only two bits in s_4 . In other words, C_1 has a higher resistance to burst errors than C_2 . Therefore, it is preferable to select C_1 for the case when QPSK single modulation is utilized for eight transmit antennas.

Figures 5(b) and 5(c) present the BERs of C_1 and C_2 in (QPSK+8PSK), (QPSK+8QAM) and (QPSK+16 QAM) MMSs. As mentioned in Section 3, for the same MMS, C_1 provides a higher code rate than C_2 . The performance of the conventional code [1] with those MMSs is presented here as the reference to evaluate the superiority of our codes (evaluation must be carried out in the same MMS, i.e., at the same bandwidth efficiency). It is noted that, for the conventional code, both symbols s_3 and s_4 are 8PSK or 16 QAM modulated in Figure 5(b), while only the symbol s_4 is 8PSK or 16 QAM modulated in Figure 5(c). The power transmitted per each symbol time slot is also normalized to one. Clearly, the MMS using an 8 QAM signal constellation provides better bit error performance than other schemes. Particularly, for the proposed codes, the SNR gains achieved by the (QPSK+8 QAM) MMS are 0.15 dB for C_2 , and 1 dB for C_1 , respectively, to have the same $BER=10^{-4}$ as in the (QPSK+8PSK) MMS. Additionally, at the same code rate, the proposed codes provide better bit error performance than the conventional code by around 3 dB in both (QPSK+8PSK) and (QPSK+16 QAM) MMSs for case of C_1 , and around 4.5 dB in (QPSK+8PSK) MMS and 5.7 dB in (QPSK+16 QAM) MMS for case of C_2 , respectively, at $BER=10^{-4}$. Therefore, at $BER=10^{-4}$, the SNR gains achieved by the (QPSK+8QAM) MMS are 4.65 dB for C_2 and 4 dB for C_1 , compared to the conventional code with the (QPSK+8PSK) MMS.

6. CONCLUSION

In this paper, the MMSs are examined to increase the rate of our proposed codes for eight transmit antennas. In addition, the authors derive the optimal inter-symbol power ratios for the proposed codes in various modulation schemes. Based on the above consideration, the following conclusions can be derived. Firstly, when QPSK single modulation is utilized, it is recommended to select the code C_1

for eight transmit antennas as it provides the best BER. Secondly, the (QPSK+8 QAM) MMS can be used to improve the performance of the codes proposed for eight transmit antennas, especially for C_1 . Thirdly, it turns out that selecting the power ratio $r=2$ for C_1 ($r=4$ for C_2) is not only optimal in terms of equal power transmission per each symbol time slot, but also optimal in terms of achieving the best symbol error property in QPSK single modulation (QPSK single modulation and (QPSK+8 PSK) MMS for C_2) in AWGN channels. Fourthly, the performance of the proposed codes can be remarkably improved, especially for the code C_1 in (QPSK+16 QAM) MMS, if the power ratio r is selected close to the optimal ratio r_{opt} , with the penalty of unbalanced power transmission per symbol time slot at a given transmit antenna. Fifthly, in the same MMS, the code C_1 may provide a higher code rate with a better error performance than C_2 if the inter-symbol power ratio is large enough, provided that the balance power transmission per each symbol time slot is not necessary property of the system. Finally, the principles examining the MMSs in order to increase the rate of STBCs and the optimal power allocation for multi-modulated STBCs mentioned in this paper can be generalized for STBCs of other orders, such as for the 4-ordered STBC in [1][7], without any difficulty.

REFERENCES

- [1] O. Tirkkonen and A. Hottinen, "Square-matrix embeddable space-time block codes for complex signal constellations," *IEEE Trans. Inform. Theory*, vol. 48, no. 2, pp. 384–395, Feb. 2002.
- [2] L. C. Tran, J. Seberry, B. J. Wysocki, T. A. Wysocki, T. Xia and Y. Zhao, "Two new complex orthogonal space-time codes for 8 transmit antennas," *IEE Electronics Lett.*, in press.
- [3] A. V. Geramita and J. Seberry, *Orthogonal designs: quadratic forms and Hadamard matrices*, Lecture notes in pure and applied mathematics, vol. 43, Marcel Dekker, New York and Basel, 1979.
- [4] G. Ganesan and P. Stoica, "Space-time block codes: a maximum SNR approach," *IEEE Trans. Inform. Theory*, vol 47, no. 4, pp. 1650–1656, May 2001.
- [5] J. G. Proakis, *Digital Communications, Fourth Edition*, McGraw-Hill, 2001.
- [6] W. T. Webb and L. Hanzo, *Modern quadrature amplitude modulation - principles and applications for fixed and wireless communications*, London: Pentech Press Limited, 1994.
- [7] Vahid Tarokh, Hamid Jafarkhani and A. R. Calderbank, "Space-time blocks codes from orthogonal designs," *IEEE Trans. Inform. Theory*, vol. 45, no. 5, July 1999.